ESSOAr | https://doi.org/10.1002/essoar.10510524.1 | CC\_BY\_NC\_ND\_4.0 | First posted online: Tue, 15 Feb 2022 08:19:21 | This content has not been peer reviewed.

# Data Fusion of AIRS and CrIMSS Near Surface Air Temperature

P. Kalmus<sup>1</sup>, H. Nguyen<sup>1</sup>, J. Roman<sup>1</sup>, T. Wang<sup>1</sup>, Q. Yue<sup>1</sup>, Y. Wen<sup>2</sup>, J. Hobbs<sup>1</sup>, and A. Braverman<sup>1</sup>

 $^1 {\rm Jet}$  Propulsion Laboratory, California Institute of Technology, Pasadena, CA, 91109 $^2 {\rm Department}$  of Geography, University of Florida, Gainesville, FL, 32611

## Key Points:

1

2

3

5 6

7

8	•	We have developed a method for fusing any number of two-dimensional remote
9		sensing datasets which estimate the same observable
10	•	We introduce a new daytime and nighttime fused near-surface air temperature
11		product from satellite hyperspectral sounders over CONUS
12	•	The fused product decreases bias and RMSE by 1 K and 25% respectively rel-
13		ative to input datasets, averaged over the domain of the study

Corresponding author: Peter Kalmus, peter.m.kalmus@jpl.nasa.gov

#### 14 Abstract

We present a near surface air temperature (NSAT) fused data product over the contigu-15 ous United States using data from the Atmospheric Infrared Sounder (AIRS), on the 16 Aqua platform, and the Cross-track Infrared Microwave Sounding Suite (CrIMSS), 17 on the Suomi National Polar-orbiting Partnership (NPP) platform. We create the 18 fused product using a fast python implementation of Spatial Statistical Data Fusion 19 (SSDF) along with weather station data from NOAA's Integrated Surface Database 20 (ISD) which is used to estimate bias and variance in the input satellite datasets. Our 21 fused NSAT product is produced twice-daily (one daytime and one nighttime estimate 22 per day) and on a 0.25-degree latitude-longitude grid. We provide detailed validation 23 using withheld ISD data and ERA5-Land reanalysis. The fused gridded product has 24 no missing data; has improved accuracy and precision relative to the input satellite 25 datasets, and comparable accuracy and precision to ERA5-Land; and includes accurate 26 uncertainty estimates. Over the domain of our study, the fused product decreases day-27 time bias magnitude by 1.7 K and 0.5 K, nighttime bias magnitude by 1.5 K and 0.2 K, 28 and overall RMSE by 35% and 15% relative to the AIRS and CrIMSS input datasets, 29 respectively. Our method is computationally fast and generalizable, capable of data 30 fusion from any number of datasets estimating the same quantity. Finally, because 31 our product removes bias, it produces long-term datasets across multi-instrument re-32 33 mote sensing records with improved stationarity for climate trend analysis, even as individual missions and their data records begin and end. 34

#### 35 1 Introduction

From the point of view of scientific analysis, satellite remote sensing datasets 36 present several challenges. Many satellite remote sensing datasets are released as 37 "Level 2" (L2) products, geophysical quantities retrieved from directly observed radi-38 ances. Instantaneous snapshots are obtained at a great number of spatial and temporal 39 fields of regard, and data coverage can be spatially incomplete due to gores (spaces 40 between orbit tracks determined by orbital and sensor geometry), clouds, downlink 41 limitations, or other issues. Satellite retrievals suffer from uncertainties and errors due 42 to information and algorithm limitations, while uncertainty estimates, if reported at 43 all, are not always reliable. Drifts of orbits and spectral channels, and even sudden 44 changes, make the use of data records from satellites challenging in climate studies 45 by causing bias nonstationarity that must be separated from real signals. While L2 46 satellite data brings invaluable information to scientific analysis, using it appropriately 47 requires significant expertise and involves serious limitations. 48

Data fusion is the combining of multiple datasets into a single dataset with better 49 properties than any of the individual input datasets (for a recent review, see Ghamisi et 50 al. (2019)). Here, we demonstrate a data fusion method, called Spatial Statistical Data 51 Fusion (SSDF) that addresses each of the above issues (Nguyen et al., 2012, 2014). We 52 use SSDF to create a fused near-surface air temperature (NSAT) product. NSAT is a 53 critical remote sensing product for climate studies of extreme heat, as well as for many 54 science applications areas of great importance to society such as health, agriculture, 55 urban planning, hydrology and water management, ecology and conservation, and fire 56 management. Our SSDF NSAT product combines two remote sensing data products: 57 L2 NSAT from the Atmospheric Infrared Sounder (AIRS) on the Aqua platform, and 58 L2 NSAT from the Cross-track Infrared Microwave Sounding Suite (CrIMSS) on the 59 Suomi National Polar-orbiting Partnership (NPP) platform, which are furthermore 60 created using two independent retrieval algorithms. We also use information content 61 from in situ weather station networks (NOAA's Integrated Surface Database, or ISD) 62 to determine uncertainties in the two remote sensing datasets which are needed to 63 perform fusion. The fused NSAT product is produced on a twice-daily basis (one

- daytime and one nighttime estimate per day), and covers the contiguous United States
   (CONUS) and adjacent parts of North America.
- Our fused SSDF NSAT product has the following key advantages over either of
   the input remote sensing datasets:
- <sup>69</sup> 1. SSDF fills spatial gaps (e.g., due to orbital gores or clouds);
  - 2. SSDF produces estimates on a regular 0.25-degree spatial grid;
  - 3. SSDF reduces bias and variance;
  - 4. SSDF produces uncertainty estimates that characterize the actual error with more skill than the input datasets;
- 5. SSDF improves long-term bias stationarity relative to the input datasets, facil itating creation of climate records over changing instrument epochs.

The rest of the paper is organized as follows. We first describe the input datasets 76 and methodology. Then we present the SSDF NSAT product, and the results of 77 validation against withheld ISD surface station data. We also compare the SSDF fused 78 NSAT product to the individual input remote sensing datasets, and to ERA5-Land 79 reanalysis. In the process of validating our SSDF product, we also produce the most 80 thorough validation study to date of the AIRS V7 and CrIMSS-CLIMCAPS V2 NSAT 81 products over CONUS. We conclude with a discussion of advantages, limitations, and 82 potential future work. 83

#### <sup>84</sup> 2 Data and methods

Performing and evaluating SSDF involves five major steps: (1) Obtaining and 85 filtering input remote sensing datasets that estimate the same quantity; (2) Matching 86 the remote sensing datasets to a reference in situ dataset in space and time; (3) Using 87 these matched data ("matchups") to characterize the input datasets via estimation of 88 their bias and variance relative to the reference estimate; (4) Performing the SSDF 89 calculations; and (5) Validating the results using withheld data from the reference 90 estimate. The method and the specific datasets used in our NSAT dataset are described 91 in the following subsections. 92

93

70

71

72

73

## 2.1 Satellite NSAT data

The input satellite datasets come from two generations of hyperspectral infrared 94 sounders and retrieval algorithms. The Aqua platform that carries AIRS launched 95 in 2002 in a sun-synchronous polar orbit, with equator crossing times of 1:30 P.M. 96 and 1:30 A.M. for ascending (south to north) and descending (north to south) nodes, 97 respectively. AIRS is an infrared grating spectrometer with 2378 channels, spanning 98 3.7 to 15.4  $\mu$ m (Chahine et al., 2006). Power to critical channels of the Aqua satellite's 99 Advanced Microwave Sounding Unit (AMSU)-A2 was lost in September 2016 (Yue 100 et al., 2017), which was used to complement the AIRS instrument in atmospheric 101 temperature and moisture profile retrievals. 102

We use the AIRS version 7 L2 "infrared-only" temperature retrieval algorithm 103 (Susskind et al., 2014). This retrieval uses the Stochastic Cloud Clearing Neural Net-104 work (SCCNN) which is trained to ECMWF fields (Blackwell, 2005) as a first guess, 105 then refines to a final estimate. It also uses information from the satellite's other mi-106 crowave sounder, AMSU-A1 (Yue et al., 2020). The retrieval uncertainty is estimated 107 via a regression model using eleven retrieval diagnostic quantities as predictors; the re-108 gression coefficients are trained on two days of retrievals (9/29/04 and 2/24/07) using 109 ECMWF 3-hour forecasts as a reference dataset (Susskind et al., 2014; Thrastarson et 110 al., 2020). Each individual retrieval has a nominal horizontal resolution of 45 km, and 111

each swath contains 30 retrievals across its width and 45 along track. The product is
organized nominally in 240 "orbital granules" per day (AIRS Project, 2020).

The Cross-track Infrared Sounder (CrIS) and the Advanced Technology Mi-114 crowave Sounder (ATMS) instruments launched onboard the NPP platform in 2012. 115 NPP is in the same orbital plane as Aqua, but at a higher altitude (824 km as opposed 116 to 705 km), with equator crossing times also nominally of 1:30 P.M. and 1:30 A.M. 117 for ascending and descending nodes, respectively. We use the Community Long-term 118 Infrared Microwave Coupled Atmospheric Product System (CLIMCAPS) Version 2 119 120 L2 temperature retrieval, which uses an optimal estimation methodology with a first guess from the Modern-Era Retrospective Analysis for Research and Applications ver-121 sion 2 (MERRA2) (N. Smith & Barnet, 2020), and information from both instruments. 122 CLIMCAPS uncertainty is estimated and propagated sequentially via error covariance 123 matrices in stages (N. Smith & Barnet, 2019). CLIMCAPS produces a combined 124 infrared and microwave retrieval at two spectral resolutions: Nominal Spectral Res-125 olution (NSR) and Full Spectral Resolution (FSR). We use the CLIMCAPS-SNPP 126 NSR product to create our SSDF product. In what follows, we refer to this product 127 as "CrIMSS-CLIMCAPS" or simply "CrIMSS." 128

For both instruments, NSAT is obtained from the vertically-resolved temperature 129 profile (100 pressure levels) by interpolation or extrapolation with pressure to the 130 surface pressure for each field of regard (Olsen et al., 2017). The profile temperatures 131 immediately above and below the surface are used for the interpolation, unless the 132 level above is within 5 hPa of the surface pressure. In that case, the two levels above 133 the surface are used. We ingest only L2 NSAT retrievals from AIRS V7 IR-only and 134 CrIMSS-CLIMCAPS products with data quality flags 'good' or 'best' in our data 135 fusion procedure. 136

137 2.2 In situ NSAT data

The National Oceanic and Atmosphere Administration (NOAA) Integrated Surface Database (ISD) is a global database of near-surface meteorological observations compiled from over a hundred sources (A. Smith et al., 2011). The record extends back to the 1950s, although new stations have been added on a continual basis as available, improving coverage over time. Today ISD consists of more than 35,000 surface weather stations globally, 14,000 of which remain active. Figure 1 shows the spatial coverage of ISD stations in North America.

We use sub-hourly 2 m NSAT measurements gathered from over 7000 stations in 145 North America as our reference dataset, for bias and variance estimation and for val-146 idation. Naturally ventilated screened surface station air temperature measurements 147 are accurate to  $\pm 0.1^{\circ}$ C in most circumstances (Harrison & Burt, 2021). ISD data come 148 with a set of ten data quality flags, indicating various problems and levels of quality. 149 We only use ISD data flagged as highest quality, i.e., data must be flagged with either 150 1 ('Passed all quality control checks') or 5 ('Passed all quality control checks, data 151 originate from an NCEI data source'). 152

### 153 2.3 Reanalysis

We also compare the SSDF NSAT results to European Centre for Medium-Range Weather Forecasts (ECMWF) Reanalysis 5 (ERA5)-Land reanalysis data. The ERA5 is the fifth-generation global atmospheric reanalysis from ECMWF, replacing the ERA-Interim reanalysis which stopped being produced on August 31st, 2019. In addition, newly reprocessed datasets along with recent instruments have been assimilated into the ERA5 that could not be ingested into the ERA-Interim (Hennermann & Berrisford, 2019). We note that some AIRS spectral channels under clear conditions are



Figure 1: Spatial coverage of the ISD stations over North America.

incorporated into ECMWF reanalysis (Mcnally et al., 2006), but that ISD data are
 not.

We use hourly ERA5-Land output which is a high-resolution version (~9 km) of the land component of the ERA5 climate reanalysis. ERA5-Land was chosen over the full ERA5 reanalysis for its finer spatial resolution of 0.1x0.1°. Hourly 2 m air temperature output was selected for our comparison.

#### <sup>167</sup> 2.4 Bias and variance estimation

Biases and variances of input data sources are crucial for proper data fusion. The SSDF methodology assumes input data are unbiased, and weights them by the inverse of their respective variances. This minimizes output errors of the fused estimates. Therefore, data are bias-corrected before SSDF ingestion, and the quality of the final fused product is largely determined by the quality of uncertainty estimates for the inputs.

To estimate bias and variance for satellite footprints, we create an ensemble 174 of "matchups": matched pairs of satellite and ISD station estimates that are close in 175 space and time. For a given period, the matchups are sorted into  $240 \,\mathrm{km}$  (~two-degree) 176 diameter hexagonal spatial bins based on satellite footprint location, with three-day 177 time bins (day of interest, along with preceding and following days). This binning 178 is the basis for quantifying bias and variance for all satellite footprints in a given 179 space-time cell. We experimented with using longer and shorter time bins to explore 180 the trade off between sample size and capturing rapid changes in conditions affecting 181 retrieval bias, and found that the three-day bin delivered the lowest average biases and 182 variances over CONUS. Before starting, we randomly selected 1% of the ISD matchups 183 to withhold for validation. We chose a relatively small amount to withhold in order to 184 maximize the information content for the SSDF product. In this subsection, the term 185 "ISD" refers to the non-withheld ISD data. 186

<sup>187</sup> To obtain the matchups we apply the following steps.

- 1. Given an ISD observation at location  $\mathbf{s}$  and time  $t^{I}(\mathbf{s})$ , select the AIRS granule (1 of 240) with the closest time to  $t^{I}(\mathbf{s})$ .
- <sup>190</sup> 2. Within this granule, select all L2 retrievals within 100 km of **s** and 1 hour of  $t^{I}(\mathbf{s})$ .
- 192

201

202

203

188

189

3. If Step 2 results in more than 1 retrieval, select the one closest in spatial distance.

Note that the Steps in 1-3 will result in a one-to-one match between an ISD observation and a single AIRS footprint. Some ISD observations may have no corresponding AIRS match, in which case we return a null result. We next tessellate a fixed hexagonal spatial grid over CONUS and find the biases and variances using matchups aggregated over 3 days within each grid cell. That is,

- I. To compute a bias on day d and mode j (day or night) and in hexagonal grid cell i, we find the set of all valid (i.e., non-null) AIRS-ISD matchups from Steps 1-3 above such that,
  - (a) the AIRS data come from mode j,
    - (b) the AIRS footprint belongs within the grid cell i,
  - (c) the ISD date is in (d-1, d, d+1).
- II. The bias and variance for day d, mode j, and grid cell i are then computed using the set of paired ISD-AIRS matchups.

Bias and variance estimation for CrIMSS follows the same procedure. For bias correction, given an instrument observation at location  $\mathbf{s}$  on day d and mode j, we compute the corresponding bias within the grid cell which contains  $\mathbf{s}$  for day d and mode j, and we subtract it from the instrument's NSAT value. For more detail on the bias and variance estimation process, please refer to the Appendix.

211 **2.5 Data fusion methodology** 

In this section we review the framework of Spatial Statistical Data Fusion (SSDF; 212 Nguyen et al., 2012) on two satellite NSAT datasets. Remote sensing data in general 213 are heterogeneous. By this we mean that they may have different footprints, mea-214 surement error characteristics, and sampling patterns. We account for this by using a 215 spatial statistical model that captures the spatial dependence between the true quan-216 tity of interest at a particular location and the observations from all data sources. In 217 particular, the issue of different footprint sizes and shapes is known as a *change-of-*218 support problem (e.g. Gotway & Young, 2002), and we will address this using SSDF 219 as described in Nguyen et al. (2012). 220

Consider a discretized domain where  $\{Y(\mathbf{s}) : \mathbf{s} \in D\}$  is a hidden, real-valued spatial observable. The domain of interest is  $\cup \{A_i \subset \Re^d : i = 1, ..., N_D\}$ , which is made up of  $N_D$  fine-scale, non-overlapping, areal regions  $\{A_i\}$  with locations  $D \equiv$  $\{\mathbf{p}_i \in A_i : i = 1, ..., N_D\}$ . Nguyen et al. (2012) call these fine-scale regions Basic Areal Units (BAUs), and they represent the smallest resolution at which we will make estimates with the model.

For a given day and mode (d and j using the notation of the previous subsection), denote the vector of NSAT data at all locations by  $\mathbf{Z}^k$ , where k = 1 for AIRS and k = 2 for CrIMSS:

$$\mathbf{Z}^{k} = (Z^{k}(B_{k1}), Z^{k}(B_{k2}), \dots, Z^{k}(B_{kN_{k}}))',$$

where  $\mathbf{Z}^k$  is  $N_k$ -dimensional,  $B_{kq}$  is the q-th footprint from the k-th dataset and is made up of BAUs with locations indexed by  $D \cap B_{kq}$ . We assume that data observed at an arbitrary areal region B follow the "data model" in which the true observable is averaged over the areal region plus an independent error term. That is,

$$Z^{k}(B) = \frac{1}{|D \cap B|} \left\{ \sum_{\mathbf{s} \in D \cap B} Y(\mathbf{s}) \right\} + \epsilon^{k}(B); \ B \subset \Re^{d}.$$
(1)

where  $Y(\cdot)$  is a geophysical observable (here, NSAT) that is common to both datasets, and  $\epsilon^k(\cdot)$  is an independent but non-identically distributed Gaussian random variable. That is, we assume that the q-th error in the k-th dataset is distributed as  $\epsilon_q^k \sim N(b_q^k, v_q^k)$ . In general,  $b_q^k$  is not zero, however, in our case  $b_q^k$  is assumed to be zero because we performed bias correction as described in the previous subsection, and  $v_q^k$  are calculated from the hexagonal-cell-specific mean and variance estimates (see Appendix for details).

Our fused estimate for a region centered at location  $B_0$  is a linear combination of  $\mathbf{Z}_1$  and  $\mathbf{Z}_2$ . That is,

$$\hat{Y}(B_0) = \mathbf{a}_1' \mathbf{Z}_1 + \mathbf{a}_2' \mathbf{Z}_2, \tag{2}$$

where  $\mathbf{a}_1$  and  $\mathbf{a}_2$  are  $N_1$  and  $N_2$  dimensional vectors, respectively. These vectors are unknown and are estimated in a way that minimizes the expected squared error relative to the true observable. That is, we choose  $\mathbf{a}_1$  and  $\mathbf{a}_2$  to minimize,

$$E((Y(B_0) - Y(B_0))^2) = \operatorname{Var}(Y(B_0) - \mathbf{a}'_1 \mathbf{Z}_1 - \mathbf{a}'_2 \mathbf{Z}_2)$$
  
= 
$$\operatorname{Var}(Y(B_0)) - 2\mathbf{a}'_1 \operatorname{Cov}(\mathbf{Z}_1, Y(B_0))$$
  
$$-2\mathbf{a}'_2 \operatorname{Cov}(\mathbf{Z}_2, Y(B_0))$$
  
$$-2\mathbf{a}'_1 \operatorname{Cov}(\mathbf{Z}_1, \mathbf{Z}_2)\mathbf{a}_2$$
  
$$+\mathbf{a}'_1 \operatorname{Var}(\mathbf{Z}_1)\mathbf{a}_1 + \mathbf{a}'_2 \operatorname{Var}(\mathbf{a}_2)\mathbf{a}_2$$

subject to the unbiasedness constraint that the elements of  $\mathbf{a}_1$  and  $\mathbf{a}_2$  add up to 1. That is,

$$1 = \mathbf{a}_1' \mathbf{1}_{N_1} + \mathbf{a}_2' \mathbf{1}_{N_2},\tag{3}$$

where  $\mathbf{1}_{N_k}$  is an  $N_k$ -dimensional vector of ones. The solution to the minimization problem in (3) can be found via the method of Lagrange multipliers; but it requires knowledge of the spatial covariance structure  $C(B_i, B_j)$ , which can be expanded in terms of the BAU covariances:

$$C(B_i, B_j) = \frac{1}{|D \cap B_i| |D \cap B_j|} \sum_{\mathbf{u} \in D \cap B_i} \sum_{\mathbf{v} \in D \cap B_j} C(\mathbf{u}, \mathbf{v}).$$
(4)

Typically, the covariance structure in kriging-based approaches is estimated from the data, but the formulation in Equation 4 makes estimation intractable for non-linear covariance classes. We make use of the Spatial Mixed Effects model (SME; Cressie & Johannesson, 2008), which assumes that the true observable, here NSAT, can be written as the linear mixed model,

$$Y(\mathbf{s}) = \mathbf{t}(\mathbf{s})'\boldsymbol{\alpha} + \mathbf{S}(\mathbf{s})'\boldsymbol{\eta} + \xi(\mathbf{s}).$$
(5)

where  $\mathbf{t}(\cdot) \equiv (t_1(\cdot), \ldots, t_p(\cdot))'$  is a vector of p known covariates, such as geographical 248 coordinates or other physical variables. The vector of linear coefficients,  $\boldsymbol{\alpha}$ , is unknown 249 and will be estimated from the data. The middle term captures the spatial dependence 250 as the product of an r-dimensional vector of known spatial basis functions,  $\mathbf{S}(\mathbf{s})$ , and an 251 r-dimensional Gaussian random variable,  $\eta$ . Here, we assume that with  $\eta \sim N(\mathbf{0}, \mathbf{K})$ . 252 Similar to the implementation in Nguyen et al. (2012), we implement these using 253 multi-resolution bisquare basis functions centered at different resolutions of the Inverse 254 Snyder Equal-Area Projection Aperture 3 Hexagon (ISEA3H) type within the Discrete 255

Global Grid (DGGRID) software (specifically, resolutions 2, 3, and 5 of ISEA3H, for details see Sahr, 2019). The last term,  $\xi(\cdot)$ , describes the BAU-scale variability of the process. We assume that  $\xi(\cdot)$  is an independent Gaussian process with mean zero and variance  $\sigma_{\mathcal{E}}^2$ .

The SME model in Equation 5 has useful change-of-support properties, which makes computation of the spatial covariance function straightforward. In particular, Nguyen et al. (2012) shows that

$$\operatorname{cov}(Z(B_i), Z(B_j)) = \mathbf{S}(B_i)' \mathbf{KS}(B_j) + \sigma_{\xi}^2 \frac{|D \cap B_i \cap B_j|}{|D \cap B_i||D \cap B_j|} + v_i^k I(i=j),$$
(6)

where

$$\mathbf{S}(B_i) \equiv \frac{1}{|D \cap B_i|} \sum_{\mathbf{u} \in D \cap B_i} \mathbf{S}(\mathbf{u}).$$

Notice that Equation 6 allows us to express the covariance between spatial averages *explicitly* in terms of the spatial dependence parameter  $\mathbf{K}$ . This allows for straightforward estimation of it from footprint data.

Another advantage of the SME model is its scalability. For a general covariance structure, solving for  $\mathbf{a}_1$  and  $\mathbf{a}_2$  requires inverting a  $(N_1 + N_2) \times (N_1 + N_2)$  covariance matrix, which has computational complexity  $O((N_1 + N_2)^3)$ . For large datasets such as AIRS and CrIMSS where the data size is on the order of tens of thousands, this matrix inversion is computationally infeasible. However, the model in Equation 5 implies the following full covariance matrix:

$$\boldsymbol{\Sigma} \equiv \operatorname{var}((\mathbf{Z}^{1\prime}, \mathbf{Z}^{2\prime})')$$
  
=  $\mathbf{S}'\mathbf{KS} + \mathbf{U},$ 

where **S** is a matrix constructed by appending the spatial function  $\mathbf{S}(\cdot)$  over all the footprints in both datasets, **U** is the *sparse* covariance matrix for the fine-scale processes  $\xi(\cdot)$ , and the measurement-error processes  $\epsilon^k(\cdot)$  at the given data locations (for more details, see Equation 4 of Nguyen et al., 2012). Using the Sherman-Morrison-Woodbury formula (e.g., Henderson & Searle, 1981), the matrix inverse is given by,

$$\Sigma^{-1} = \mathbf{U}^{-1} - \mathbf{U}^{-1} \mathbf{S}' \left( \mathbf{K}^{-1} + \mathbf{S} \mathbf{U}^{-1} \mathbf{S}' \right)^{-1} \mathbf{S} \mathbf{U}^{-1},$$

Note that the inversion above, and hence the calculation of the coefficients  $\mathbf{a}_1$  and  $\mathbf{a}_2$  for the fused estimate, is very fast because it only requires inversion of the *sparse*   $(N_1 + N_2) \times (N_1 + N_2)$  matrix  $\mathbf{U}$ , which is typically very sparse, and inversion of  $\mathbf{K}$ and  $(\mathbf{K}^{-1} + \mathbf{S}'\mathbf{U}^{-1}\mathbf{S})$ , both of which are  $r \times r$  matrices  $(r << N_1 + N_2)$ .

The methodology described in this section is a scalable variant of Gaussian process prediction (Cressie, 2015). It has been applied to fusion of total column CO<sub>2</sub> concentration (XCO2) from AIRS and OCO-2 and aerosol optical depth from MISR and MODIS (Nguyen et al., 2012, 2014). Hammerling et al. (2012) used another variant called local kriging to produce Level 3 estimates of XCO2 from the GOSAT instrument.

There are two important advantages of Gaussian process prediction over other 287 approaches currently in use such as binning or nearest neighbor interpolation. First, 288 our fused estimates are best linear unbiased estimates. That is, the standard errors are 289 guaranteed to be the smallest possible because the estimates are derived through an 290 algorithm that minimizes errors relative to the unknown true process. Such estimates 291 are called best linear unbiased estimates, and are optimal in that sense. It is easily 292 shown that within the class of linear estimators, this method produces the smallest 293 prediction errors. The second advantage is that SSDF provides a statistically princi-294 pled method for estimating uncertainties (that is,  $\operatorname{Var}(Y(B_0) - Y(B_0))$ ). Quantifying 295 and minimizing uncertainties in this manner is crucial for creating data products for 296 scientific analyses that involve making inferences about geophysical observables. 297

### 298 2.6 Dataset preparation for validation

We validate our SSDF product using a randomly chosen reserved 1% of the ISD 299 dataset. We match up SSDF, AIRS, CrIMSS, and ERA5 estimates to withheld ISD 300 data using a 100 km and 1 hour matchup criterion (see Section 2.4 for more detail). 301 This matchup procedure generates multiple paired datasets: ISD-AIRS, ISD-CrIMSS, 302 ISD-SSDF, and ISD-ERA5. These matchup datasets might differ in their coverage; 303 for instance, an SSDF estimate might be matched to an ISD observation at a location 304 where there are no nearby AIRS or CrIMSS estimates. Therefore, to mitigate the effect 305 of biases due to differing spatial and temporal coverage in these matchup pairs, we also 306 require that SSDF estimates are also close to (within the same matchup distance and 307 time) at least one datum from the comparison dataset. This allows us to compare, for 308 example, AIRS and SSDF(AIRS) datasets which have the same number of samples, 309 all of which are collocated in space and time within the matchup criterion. 310

The choices of a 1% test ISD dataset and this matchup scheme results in over 4000 AIRS-SSDF sample pairs and over 13,000 CrIMSS-SSDF sample pairs for 2013, a typical year.

#### 314 **3 Results**

315

#### 3.1 SSDF product overview

We produced fused NSAT using two satellite input datasets over North America 316 between 25 N and 50 N, from November 28 2012, when CrIMSS-CLIMCAPS first 317 becomes available, through the end of 2020. During this time period, there were 34 318 days and 36 nights with no AIRS data (approximately half of which occurred in 2020), 319 and 24 days and 28 nights with no CrIMSS-CLIMCAPS data. In the cases with only 320 one input satellite dataset, the SSDF product is created from only the single dataset, 321 thus creating a continuous record. There was one day/night period (November 7, 2020) 322 without either AIRS or CrIMSS-CLIMCAPS data; we did not create SSDF product 323 for this day. 324



Figure 2: Sample data fusion satellite NSAT inputs, SSDF NSAT results, and uncertainty estimates for 2015 October 31, day. The top two plots show maps of the input satellite NSAT data ingested into the SSDF product, with AIRS on the left and CrIMSS on the right. The bottom-left plot shows the SSDF fusion results. The bottom-right plot shows the uncertainty estimates on the SSDF fusion results at the 1-sigma level. All units are Kelvin.



Figure 3: Same as Figure 2 but for night. All units are degrees K.

Figures 2 and 3 provide maps representing one arbitrarily chosen day and night 325 of the SSDF product. For both the day and night cases, the top two plots show maps 326 of the input satellite data ingested into the SSDF product, with AIRS on the left and 327 CrIMSS on the right; the bottom left plot shows the SSDF fusion results; and the 328 bottom right plot shows the uncertainty estimates on the SSDF fusion results at the 329 1-sigma level. These sample maps demonstrate how our SSDF method fills in missing 330 data in the input datasets by exploiting spatial correlations to provide a complete 331 gap-filled, gridded product. They also provide a first look at the SSDF uncertainty 332 estimates. Note that the estimated uncertainties are higher in regions that contain no 333 observations, contain observations from only a single input dataset, or in which the 334 two input datasets have relatively poor agreement. 335

336

## 3.2 Bias, standard deviation, and RMSE comparison

We now turn to validation against withheld ISD reference data to quantify improvement in the SSDF products. We examine bias, standard deviation, and RMSE, calculated from the withheld matchups, of AIRS, CrIMSS, ERA5-Land, and the corresponding matched SSDF data. In what follows, analyze daytime and nighttime separately, as daytime and nighttime biases differ significantly.

We first show maps of bias, RMSE, and standard deviation relative to the 1% of withheld (testing-only) ISD reference data, based on the matchups aggregated into the hexagonal bins. Figure 4 shows maps of bias (retrieval - ISD) for AIRS, CrIMSS, and SSDF, for the 2013-2020 period in total, and for day-only and night-only. Individual bias estimates for retrieval-ISD pairs are aggregated into 2-degree hexagonal cells.

Overall, in the mean over CONUS and over the entire time period, SSDF provides a reduction in the magnitude of daytime bias of 1.7 K and 0.5 K relative to AIRS and CrIMMS, respectively. At night, SSDF is essentially unbiased in the mean over the domain and provides a reduction in the magnitude of bias of 1.5 K and 0.2 K relative to AIRS and CrIMMS, respectively.

AIRS shows a strong cold bias in daytime over the mountainous West, which is also present in CrIMSS, although less severe. AIRS shows a near-constant warm bias over the entire Eastern CONUS at night, while CrIMSS shows a sharp warm bias over small regions of the mountainous West at night. SSDF corrects all of these biases (through the bias-correction procedure described above) and produces estimates with lower biases than either of its input satellite data sets over the domain.



Figure 4: Maps of bias (retrieval - ISD) over the product period of 2013-2020, created against the withheld ISD test data, for AIRS (first column), CrIMSS-CLIMCAPS (second column) and SSDF (third column), for both day and night together (top row), for day only (second row) and for night only (third row). Individual bias estimates for retrieval-ISD matchup pairs are aggregated over 2-degree hexagonal cells. The mean bias over CONUS for the entire time period is shown in the title for each map.

Figures 5 and 6 show maps of standard deviation and RMSE for AIRS, CrIMSS and SSDF, for the 2013-2020 period, and for daytime only and nightime only. Standard deviation and RMSE tell a similar story to that of bias. Overall, in the mean over CONUS and over the entire time period, SSDF provides a reduction in RMSE of 35% and 15% compared to AIRS and CrIMSS, respectively.

CrIMSS has high RMSE over the mountainous West in both day and night, 363 but low RMSE over the eastern two-thirds of the continent. Similarly, AIRS has 364 relatively high RMSE over the entire domain, but especially over the mountainous 365 West. Mountainous regions pose particular challenges for remote sensing of surface 366 quantities, and of NSAT in particular, which can vary greatly depending on e.g., north-367 facing versus south-facing mountain surfaces. Furthermore, variations in topographic 368 features between ISD stations and their matched remote sensing retrievals can lead 369 to random errors, increasing RMSE and variance estimates. However, SSDF NSAT 370 shows a clear decrease in bias over all regions, including in the mountainous western 371 CONUS, although there is potential for improvement in the SSDF product over the 372 West. 373



Figure 5: Standard deviation maps. The nine panels are similar to those in Figure 4 but for standard deviation.



Figure 6: RMSE maps. The nine panels are similar to those in Figure 4 but for RMSE.

We repeated this analysis over CONUS and the 2013-2020 period for the SSDF product created with AIRS alone, without CrIMSS. We found similar improvements in bias, standard deviation, and RMSE. The mean bias of the AIRS-only SSDF product over the entire domain was -0.08 K for daytime only, and -0.03 K for nighttime only. The overall RMSE was 2.52 K, 4% higher than the overall RMSE of the SSDF product created from both AIRS and CrIMSS.

Figure 7 shows histograms of the NSAT error (retrieval/reanalysis - ISD) for the 380 year 2013, over CONUS only. The three comparison datasets (AIRS, CrIMSS, and 381 ERA5-Land) were matched separately to SSDF outputs, to ensure that the SSDF 382 product and each corresponding comparison dataset are considering the same scenes. 383 The SSDF error histograms are symmetric with a single mode and peak at 0 for both 384 day and night, which is consistent with the errors being unbiased. The AIRS histogram 385 exhibits a cold bias during the day and a warm bias at night. CrIMSS has a similar 386 day/night bias shift, but of a smaller magnitude. A cold bias over land, particularly 387 at higher temperatures, has been previously noted for both input datasets (Yue et al., 388 2020, 2021), although there have been few validation studies (Ferguson & Wood, 2010; 389 Sun et al., 2021). The SSDF product exhibits smaller mean biases and RMSEs than 390 either input dataset. On average, over both input datasets, daytime and nighttime, 391 SSDF decreases mean bias magnitude by 81% and mean RMSE by 23% relative to the 392 input datasets. 393

Next, we examine the seasonality of bias and RMSE. Figure 8 shows the mean 394 bias (retrieval/reanalysis – ISD) by month split into day/night to examine seasonality. 395 There is a significant cold bias during the day for AIRS and CrIMSS that switches 396 to a warm bias at night. During the day, AIRS has a smaller bias during winter 397 months (Dec/Jan/Feb) and a larger bias during summer months (Jun/Jul/Aug). This 398 is switched during nighttime where a larger warm bias is observed during winter and 399 a smaller warm bias is observed during summer. These AIRS biases are of course also 400 apparent in Figure 7. The SSDF product is relatively unbiased for both day and night. 401 The SSDF bias magnitude is slightly larger during the day than night. From May to 402 December, the SSDF product has a smaller bias at night than does ERA5-Land while 403 during the day the reanalysis and the SSDF mean biases are of similar magnitude. 404

Figure 9 shows mean RMSE (retrieval/reanalysis – ISD) by month split by day/night,
i.e., the mean RMSE values calculated in 2-degree spatial bins. RMSE is largest for
AIRS, particularly during the day. Generally, RMSE is higher in winter and lower in
summer. During the day, the ERA5-Land has the lowest RMSE. At night, the SSDF
RMSE is comparable and sometimes lower than the ERA5-Land RMSE.

We next examine relative performance in hot and cold extremes. Figure 10 shows 410 the mean bias (retrieval/reanalysis – ISD) by ISD percentile of the ISD matchups. The 411 error bars are the standard error of the mean at the 95 percent confidence level. The 412 lighter shade of every color is the matched SSDF corresponding to the comparison 413 dataset. All retrievals and reanalysis do best in the mean state (25th to 75th per-414 centile). At the extremes, each of the datasets being compared to ISD have warm 415 biases for low values (1st through the 15th percentile) and cold biases for high val-416 ues (85th through the 99th); in other words, these datasets dampen out capture cold 417 or warm extremes represented in the ISD. The SSDF product captures the extremes 418 better than the input datasets, AIRS and CrIMSS. However, the reanalysis generally 419 does best, having the smallest bias regardless of percentile, and is better at capturing 420 the extremes. 421

We next examine performance at extremely high elevations. Figure 11 shows mean biases (retrieval/reanalysis – ISD) aggregated by ISD elevation. At around 2500 meters, mean biases increase with elevation in the SSDF product, AIRS, CrIMSS, and reanalysis. Daytime mean biases at these high elevations are larger in SSDF, although



Figure 7: Histograms of errors for day (top) and night (bottom) for 2013 over CONUS, for AIRS (blue), CrIMSS (red) and ERA5-Land (green). The dashed line is the SSDF subset matched to the other datasets. Mean statistics of bias, RMSE, and the number of samples are provided.

we note that the sample size is small. At night, SSDF shows lower mean biases than AIRS, CrIMSS, or ERA5-Land at high elevations.

In order to increase the sample size for high-elevation cases, Figure 12 shows 428 the mean biases aggregated by ISD elevation for elevations higher than 2000 meters 429 over the period 2012-2020. During the day, the SSDF bias exceeds AIRS and CrIMSS, 430 consistent with Figure 11. We hypothesize that this excess bias in SSDF for a very small 431 number of data points at very high elevations is caused by the bulk-binning method 432 for bias estimation. As Figure 11 shows, both remote sensing datasets exhibit a cold 433 bias during the daytime at lower elevations. Because the two-degree hexagonal bins for 434 bias estimation are dominated by lower elevations (as the problematic high elevations 435 are high mountain surfaces), and because both remote sensing dataset biases switch 436 signs from cold bias to warm bias at approximately 2500 m, the cold bias correction 437 calculated from the bulk bins ends up exacerbating the warm bias from the input 438 datasets at the highest elevations. In a future version of SSDF, we will improve the 439

manuscript submitted to Earth and Space Science



Figure 8: Mean bias as a function of month for day (top) and night (bottom) for 2013 over CONUS. Numbers at the bottom indicate the number of data points, and are color-coded according to dataset.

- bias estimation of the input datasets, which could mitigate or eliminate this bias at
- the very small number of estimates elevations above 2500 m.

manuscript submitted to Earth and Space Science



Figure 9: Mean RMSE as a function of month for day (top) and night (bottom) for 2013 over CONUS. Numbers at the bottom indicate the number of data points, and are color-coded according to dataset.



Figure 10: Mean biases as a function of ISD percentile for 2013 over CONUS. Numbers at the bottom indicate the number of data points, and are color-coded according to dataset.



Figure 11: Mean biases as a function of ISD elevation for day (top) and night (bottom) for 2013 over CONUS. Numbers at the top indicate the number of data points, and are color-coded according to dataset.



Figure 12: Mean biases as a function of ISD elevation for day (top) and night (bottom) over CONUS from 2012-2020 for AIRS, CrIMSS, and SSDF. Numbers at the top indicate the number of data points, and are color-coded according to dataset.

#### **3.3** Validation of uncertainty estimates

451

452

453

454

455

456

The SSDF algorithm provides a mean (prediction/estimate) and standard devi-443 ation (uncertainty) of the conditional distribution of true NSAT, given the available 444 inputs; this distribution is termed the predictive distribution. In what follows, this 445 is a Gaussian distribution, centered at the SSDF estimate. This information can be 446 used to construct prediction intervals for the true NSAT. Here we provide a summary 447 and probabilistic assessment of the SSDF predictive distribution along with related in-448 formation from the AIRS V7 and CrIMSS-CLIMCAPS V2 products. In the notation 449 that follows, we use the subscript i in place of the areal unit notation  $B_i$ . 450

- In addition to each SSDF NSAT estimate,  $\hat{Y}_i$ , the algorithm also provides the conditional standard deviation of the predictive distribution, denoted  $\hat{\sigma}_{\hat{Y}_i}$ .
- The AIRS V7 NSAT retrieval,  $Z_{1,i}$ , is accompanied by a corresponding uncertainty estimate, denoted  $\hat{\sigma}_{Z,1,i}$  (Susskind et al., 2014). This estimate results from a regression model for predicting the absolute retrieval error given several predictors available from the retrieval.
- The CrIMSS-CLIMCAPS V2 retrieval,  $Z_{2,i}$ , also has a corresponding uncertainty estimate, denoted  $\hat{\sigma}_{Z,2,i}$  (N. Smith & Barnet, 2020). This estimate results from a linear approximation of the posterior standard deviation of the true state given the observed radiances for a single footprint and is an output of the optimal estimation (OE) approach used in CLIMCAPS.

Figure 13 shows histograms of these uncertainty estimates:  $\hat{\sigma}_{Z,1}$ ,  $\hat{\sigma}_{Z,2}$ , and  $\hat{\sigma}_{\hat{Y}}$ across the CONUS data record. The solid line shows uncertainty estimates from AIRS (blue) and CrIMSS (red) while the dashed shows the corresponding matched SSDF uncertainty estimates. CrIMSS has a peak around 1.2 K with a narrow distribution; AIRS V7 has a peak between 1.5 and 2 K with a wide distribution. SSDF uncertainty histograms peak around 2 K.

These uncertainty estimates are properties of distributions, whereas we define error  $e_i$  as a realization of a random variable that represents the difference between an estimate and the true state. For example, the error for SSDF is  $e_{\hat{y},i} = \hat{Y}_i - Y_i$ , where  $Y_i$  is the ISD validation for colocation *i*. If the predictive distribution is assumed to be Gaussian, the empirical coverage of intervals of the form

$$\hat{Y}_i \pm c \,\hat{\sigma}_{\hat{Y},i},$$

can be assessed for the ISD matchups. In the case of an unbiased estimate, "wellcalibrated" uncertainty estimates, and a Gaussian distribution; intervals with c = 1should cover the true state  $Y_i$  about 68% of the time, and about 95% of the time for c = 2.

Figure 14 shows scatterplots of the joint distribution of the uncertainty estimate 472 (x-axis) and the observed error (retrieval-ISD). There are many cases for AIRS and 473 CrIMSS where the uncertainty estimate grossly underestimates the true error; over 474 15% of the time for both datasets and for day and night, the true error is more than 475 three times greater than the uncertainty estimate. However, this occurs about 3% of 476 the time with SSDF in the day and fewer than 5% of the time at night. Overall, the 477 CrIMSS uncertainty estimates are distributed too narrowly, and with a peak too low, 478 to capture the true error. The AIRS uncertainty estimates also peak at a value below 479 the peak of the error distribution, although the uncertainty estimate distribution is 480 much wider, including a very long tail of high uncertainty estimates. 481

In general, SSDF uncertainty estimates are consistent with statistical expecta tions under Gaussian assumptions. For example, one would expect one-sigma uncer tainty estimates to cover a standard error distribution 68% of the time, and we see

manuscript submitted to Earth and Space Science

ESSOAr | https://doi.org/10.1002/essoar.10510524.1 | CC\_BY\_NC\_ND\_4.0 | First posted online: Tue, 15 Feb 2022 08:19:21 | This content has not been peer reviewed.



Figure 13: Histograms of uncertainty estimates for day (top) and night (bottom) for 2013 over CONUS.

- that the SSDF uncertainty estimates do so roughly 65% of the time in daytime. Simi-485
- larly, one would expect the estimates to cover 95% and over 99% at the 2- and 3-sigma 486
- levels, with SSDF covering about 90% and 97% during daytime. 487



Figure 14: Observed errors (retrieval - ISD) versus uncertainty estimates for day (top) and night (bottom) for 2013 over CONUS. The colors show whether the range of each observed error was within the uncertainty bound, as described in the text:  $1 \times$  uncertainty (green, should cover the true state about 68% of the time),  $2 \times$  uncertainty (orange, should cover the true state about 95% of the time),  $3 \times$  uncertainty (red, should cover the true state about 99% of the time) or  $> 3 \times$  uncertainty (black).

### 488 **3.4 Empirical distribution consistency**

The ISD record provides a sample of the empirical distribution of NSAT over 489 CONUS. Here, we assess the relative consistency of the SSDF empirical distribution 490 versus the other products against the ISD reference distribution. Figure 15 shows an 491 example of the empirical cumulative distribution (ECDF) for the ISD (pink) and AIRS 492 (blue). While it is almost certainly the case that the products' ECDFs deviate from the 493 ISD reference distribution in some subtle ways, we evaluate their relative consistency 494 with ISD through a series of hypothesis tests. Figure 16 shows the difference between 495 the ECDF of the retrieval/reanalysis to the ECDF of ISD. The AIRS ECDF has the largest difference to the ISD ECDF, particularly during the Day. 497

![](_page_22_Figure_3.jpeg)

Figure 15: ECDF for AIRS (blue) and ISD (pink) for day (top) and night (bottom) for 2013 over CONUS.

The SSDF estimates are tested against each of the other products (AIRS, CrIMSS, ERA5-Land) for night and day conditions. Each assessment is carried out using a randomization or resampling test (Wilks, 2006). For this test, the null hypothesis is that the empirical distributions of SSDF and the comparison product deviate equally from the ISD reference distribution. The alternative hypothesis is that either SSDF or the comparison product have an empirical distribution that is closer to the ISD reference distribution. For this procedure, the test statistic is computed as the difference in two-sample Kolmogorov-Smirnov (KS) statistics for the products versus ISD.

For each instance of the test, we have a collection of matched triples  $\{\hat{\mathbf{Y}}, \mathbf{Z}_k, \mathbf{Y}\}$ ; where  $\hat{\mathbf{Y}} \equiv \{\hat{Y}_i\}$ ; i = 1, ..., n are the SSDF estimates,  $\mathbf{Z}_k \equiv \{Z_{k,i}\}$ ; i = 1, ..., n are the comparison products, and  $\mathbf{Y} \equiv \{Y_i\}$ ; i = 1, ..., n are the ISD NSAT. As above, k = 1 for AIRS, k = 2 for CrIMSS, and here k = 3 for ERA5-Land. Then, test k has a test statistic

$$\gamma_k = \delta(\mathbf{Y}, \mathbf{Y}) - \delta(\mathbf{Z}_k, \mathbf{Y}),$$

where  $\delta$  is the traditional two-sample KS statistic. The KS statistic is the maximum difference in the two ECDFs being compared. Thus, the test statistic  $\gamma_k$  for the current test is a *difference* of ECDF deviations. A negative value is an indication that the SSDF distribution is closer to ISD than the comparison product.

![](_page_23_Figure_1.jpeg)

Figure 16: The ECDF difference between the retrieval/reanalysis and the ISD color coded for day (top) and night (bottom) for 2013 over CONUS.

The distribution of the test statistic under the null hypothesis can be established through a resampling procedure. The procedure should preserve the inherent dependence of the matched triples, but the assignment of the two comparison groups can be shuffled randomly. A null distribution is generated by repeating these steps m = 1, ... M times:

- 1. Define shuffled data vectors  $\mathbf{W}_{m,1}$  and  $\mathbf{W}_{m,2}$ .
- 2. For each validation matchup  $(i = 1, ..., n_k)$ , assign  $W_{i,m,1} = \hat{Y}_i$  and  $W_{m,2,i} = Z_{k,i}$  with probability 0.5; otherwise assign  $W_{m,1,i} = Z_{k,i}$  and  $W_{i,m,2} = \hat{Y}_i$ . This effectively shuffles the labels for SSDF and the comparison product for each matchup.
  - 3. Compute the test statistic for the randomized samples,

$$\gamma_{0,m,k} = \delta(\mathbf{W}_{m,1}, \mathbf{Y}) - \delta(\mathbf{W}_{m,2}, \mathbf{Y}),$$

The distribution of  $\gamma_{0,m,k}$  provides the null distribution of the test statistic for each test. Figure 17 displays the test statistics  $\gamma_k$  along with density plots of the null distributions of test statistics  $\gamma_{0,m,k}$  for M = 20,000 resampled datasets for each test. A two-sided *p*-value can be computed for each test as

$$p_k = \frac{1}{M} \sum_{m=1}^M I_{\gamma}(|\gamma_{0,m,k}| > |\gamma_k|),$$

s20 where  $I_{\gamma}$  is an indicator function.

515

The *p*-values for each of the resampling tests of SSDF versus other products are 521 displayed as text in Figure 17. All tests, except the night comparison of SSDF and 522 CrIMSS, yield *p*-values of 0, indicating a significant difference in consistency with the 523 ISD reference distribution. These results can also be seen visually as the observed test 524 statistics  $\gamma_k$ , shown as vertical lines, lie well outside the corresponding null distribu-525 tions. The tests indicate SSDF is more consistent with ISD than AIRS for both day 526 and night conditions, as well as a favorable result for SSDF versus CrIMSS for day and 527 versus ERA5-Land at night. The positive test statistic for SSDF versus ERA5-Land 528 during the day indicates the reanalysis is more consistent with ISD in this case. 529

![](_page_24_Figure_2.jpeg)

Figure 17: Histogram of the KS statistic for AIRS (blue), CrIMSS (maroon) and ERA5-Land (green), for day (top) and night (bottom) for 2013 over CONUS. The corresponding p-value is color-coded on the left side.

530

# 3.5 Long-term stationarity

We next assess the stationarity in the bias of the SSDF dataset. First, we exam-531 ine the annual mean bias over the entire record relative to the withheld ISD reference 532 data. Figure 18 shows the annual mean bias (both day and night) for both the input 533 datasets, as well as for two periods of SSDF: the pre-CrIMSS period (2003 to 2011, 534 inclusive) and the post-CrIMSS period (2013 to 2020, inclusive). Shading shows two 535 standard deviations of these annual bias estimates, with the two SSDF periods calcu-536 lated separately. We exclude 2002 as this year only includes 4 months of AIRS data, 537 and we exclude 2012 as this year was a mixture of AIRS-only and AIRS-plus-CrIMSS. 538

These summary data clearly show that SSDF significantly improves both the mean annual bias, and the standard deviation in mean annual bias, relative to the

input datasets. The mean of these annual bias estimates are  $-0.10^{\circ}$ C,  $-0.23^{\circ}$ C, and 541 0.02°C for AIRS, CrIMSS, and SSDF respectively, from 2003 to 2020 inclusive for 542 AIRS and SSDF and from 2013 to 2020 inclusive for CrIMSS. However, these data 543 also suggest a step change in SSDF mean annual bias in the pre-CrIMSS and post-544 CrIMSS period. The mean of the SSDF mean annual bias estimates in the pre-CrIMSS 545 and post-CrIMSS periods are -0.020°C and 0.076°C, respectively, a shift of about 0.1°C. 546 This shift is small compared to the biases in the input remote sensing datasets, and the 547 apparent downward trend in the AIRS dataset. Over-correction with the addition of 548 the CrIMSS dataset might be an artifact of the bias estimation bulk-binning procedure. 549 This small step change in bias does not occur in the AIRS-only SSDF product over the 550 full AIRS record. Future versions of SSDF will use improved uncertainty quantification 551 methods to estimate input dataset biases, which could mitigate or eliminate this small 552 shift in annual mean bias in transitioning from the AIRS-only SSDF product to the 553 two-instrument product. In the meantime, the first version of our product creates a 554 more coherent and stable climate record than the two input datasets taken separately. 555

![](_page_25_Figure_2.jpeg)

Figure 18: Annual mean bias for each year of the data record, for the SSDF product and each of the two remote sensing input products, relative to the withheld ISD data. Shading shows two standard deviations of these annual bias estimates, with the two SSDF periods calculated separately.

Figure 19 shows the histogram of the SSDF uncertainty estimates for 2011 (black) and 2013 (red). The mean uncertainty is provided as text. The histograms are comparable. The 2011 (single instrument only) histogram is shifted slightly to the right suggesting higher uncertainty estimates with one instrument compared to two. Indeed, the mean SSDF uncertainty estimate is 2.15/2.21 (Day/Night) during 2011 and decreases to 2.12/2.09 in 2013. However, this is to be expected as the additional information from CrIMSS provides greater certainty for SSDF.

![](_page_26_Figure_1.jpeg)

Figure 19: SSDF uncertainty histogram for 2011 (black) and 2013 (red) aggregated by day (top) and night(bottom). Summary statistics of mean SSDF uncertainty are provided as text on the upper left.

## <sup>563</sup> 4 Discussion and conclusion

We have produced a new fused NSAT product over CONUS, from November 2012 564 through December 2020, using Spatial Statistical Data Fusion of AIRS and CrIMSS 565 remotely sensed NSAT. We also provided detailed validation using withheld ISD data, 566 and comparison to ECMWF ERA5-Land reanalysis. Remote sensing data provides 567 information to span the spatial domain, in situ data provides the information to correct 568 the remote sensing data, and SSDF provides the means to join them into something 569 greater than the sum of their parts. The fused gridded product has no missing data 570 571 (apart from one day and night without either AIRS or CrIMSS-CLIMCAPS input data); has improved accuracy and precision relative to the input satellite datasets, has 572 comparable accuracy and precision relative to to ERA5-Land and indeed significantly 573 lower nighttime bias than ERA5-Land; and includes estimates that are more consistent 574 with the observed errors relative to in situ ISD observations. To summarize, our 575 NSAT SSDF pilot product is comparable in precision and accuracy to the cutting-576 edge ERA5-Land reanalysis, but it is a direct observational product that does not 577 involve physical modeling. Furthermore, unlike reanalysis it could support near-real-578 time product creation for operational applications. 579

SSDF is general and could be applied to any number of datasets estimating the
same observable. It could be applied across a wide range of satellite observables, such as
atmospheric composition, water vapor profiles, or vapor pressure deficit (the difference
between the water vapour pressure and the saturation water vapour pressure), so long
as uncertainty estimates of the input datasets can be obtained. We emphasize that the
quality of the SSDF product depends on the quality of the bias and variance estimates
of the input datasets.

Our plans for future work include improving the bias and variance estimation 587 using simulation-based uncertainty quantification (Hobbs et al., 2017; Braverman et 588 al., 2021). Simulation-based uncertainty quantification has the potential to further 589 improve the overall quality of the SSDF product. It could also mitigate or eliminate 590 the two issues our validation has uncovered: increased bias at a small number of 591 data points at elevations in excess of 2500 m, and a 0.1 K shift in annual mean 592 bias when transitioning from the AIRS-only version (2002-2012) to the two input 593 (AIRS+CrIMSS) SSDF version (2012-2020). 594

We also plan to create an NSAT SSDF product over global land areas, expanding beyond CONUS, and apply the SSDF method to other hyperspectral surface products (e.g., vapor pressure deficit). Finally, we plan to develop SSDF products for satellite instruments that sample observables at different points in the diurnal cycle, to enable fusion of datasets from polar-orbiting and inclined platforms to make optimal use of all available remote sensing.

## 601 Open Research

The SSDF NSAT dataset described in this paper is available at http://dx.doi.org/10.5067/CPXNAPA2WSQ8.

Publicly available data were obtained from the NASA Atmospheric Infrared Sounder and the Suomi-NPP projects, the NOAA Integrated Surface Databse, and the European Centre for Medium-Range Weather Forecasts reanalysis.

Aqua AIRS V7 is available from the NASA GES DISC repository (AIRS Project,
 2019). The retrieved surface air temperature (TSurfAir), the corresponding error es timate for TSurfAir (TSurfAirErr), and the corresponding quality flag (QC) (TSurfAir\_QC) were obtained for the standard IR-only product.

CrIMSS-CLIMCAPS V2 is available from the NASA GES DISC repository (Barnet,
 2019). Near surface temperature (surf\_air\_temp), the corresponding QC flag (surf\_air\_temp\_qc),
 and the corresponding error estimate (surf\_air\_temp\_err) were obtained from the NSR
 product.

NOAA ISD NSAT data is available using the rnoaa R package.

ECMWF ERA5-Land gridded hourly 2 m temperature means are available from the Copernicus Climate Change Service (C3S) Climate Data Store (Copernicus 2017).

#### 618 Acknowledgments

615

The research was carried out at the Jet Propulsion Laboratory, California Institute of Technology, under a contract with the National Aeronautics and Space Administration (80NM0018D0004). We thank Evan Fishbein, Evan Manning, Erik Fetzer, and Bjorn

Lambrigtsen for helpful discussions. ©2022

## <sup>623</sup> Appendix A Matchups and bias estimation

In this section, we will elaborate in detail our procedure for matching between 624 ISD and the instruments' observations, and the consequent bias estimation process. 625 For clarity, we establish the following notation. Let  $\mathbf{s}$ ,  $\mathbf{u}$ , and  $\mathbf{v}$  be latitude-longitude 626 locations; e.g.,  $\mathbf{s} = (lat, lon)$ . On a given day (or night) let  $Z^k(\mathbf{u})$  be the value of 627 the k-th instrument's near-surface temperature retrieval centered at  $\mathbf{u}$ . and focus on 628 a single ISD station at location **s** during a single period. Let  $t_1^I(\mathbf{s}), \ldots, t_M^I(\mathbf{s})$  be the 629 times at which observations are acquired at this station during the period. These time 630 points may be irregularly spaced, and M can change from station to station. The ISD 631 measurements are  $Z^{I}(\mathbf{s}, Z_{m}^{I}(\mathbf{s})), m = 1, \dots, M.$ 632

Let  $t^{k}(\mathbf{u})$  be the acquisition times associated with the k-th instrument's footprints centered at location  $\mathbf{u}$ . In principle,  $\mathbf{u}$  ranges over all footprint locations for the appropriate instrument during the entire period, but in practice these locations are grouped by granules. We denote granule number during the current period by g = $1, \ldots, 120$ , and the set of footprints belonging to granule g by  $\mathcal{G}_{g}^{k}$ . The time associated with  $\mathcal{G}_{g}^{k}$  is  $\tau_{g}^{k}$ . To ease the computational burden,  $\mathbf{u}$  ranges only over locations in the single granule with time that is closest to  $t_{m}^{I}(\mathbf{s})$ .

A matchup associates the location and time of an ISD value,  $(\mathbf{s}, t^{I}(\mathbf{s}))$ , with the location and time of the k-th instrument's footprint in the period:  $(\mathbf{u}^{*}, t^{k}(\mathbf{u}^{*}))$ . The matchup function is,

$$\begin{split} \mathbb{M}^{k}\left(\mathbf{s}, t_{m}^{I}(\mathbf{s})\right) &= \left(\mathbf{u}^{*}, t^{k}(\mathbf{u}^{*})\right), \\ \mathbf{u}^{*} &= \operatorname*{argmin}_{\mathbf{u}} \left\{ ||\mathbf{u} - \mathbf{s}||, \, \mathbf{u} \in \left(\mathcal{G}_{g^{*}}^{k} \cap \mathcal{U}^{time} \cap \mathcal{U}^{space}\right) \right\}, \\ g^{*} &= \operatorname*{argmin}_{g} \left\{ \left|\tau_{g}^{k} - t_{m}^{I}(\mathbf{s})\right| \right\}, \\ \mathcal{U}^{time} &= \left\{\mathbf{u} : \left|t^{k}(\mathbf{u}) - t_{m}^{I}(\mathbf{s})\right| \leq 1 \text{ hour} \right\}, \, \mathcal{U}^{space} = \left\{\mathbf{u} : ||\mathbf{u} - \mathbf{s}|| \leq 100 \text{ km} \right\}. \end{split}$$

640 641 Note that, for a given instrument and period, there will only be one granule that satisfies the criterion provided by  $g^*$ .

For a given ISD station (indexed by location  $\mathbf{s}$ ) in the current period, p, we create the sets of matchup values for the k-th instrument as follows,

$$\mathcal{A}^{k}(p,\mathbf{s}) = \left\{ Z^{I}\left(\mathbf{s}, t_{m}^{I}(\mathbf{s})\right), \, Z^{k}\left(\mathbb{M}^{k}\left(\mathbf{s}, t_{m}^{I}(\mathbf{s})\right)\right) \right\}_{m=1}^{M(p,\mathbf{s})}$$

for all ISD time points at **s** indexed by  $m = 1, ..., M(p, \mathbf{s})$ . p is identified by a date and a mode (day/night) indicator, e.g., p = (d, j) = (2013-01-01, day).  $M(p, \mathbf{s})$  is the number of ISD station values in period p at location  $\mathbf{s}$ . There is at most one AIRS and one CrIMSS footprint associated with each station-time, but the same footprint can be associated with more than one station-time. Thus,  $\mathcal{A}^k(p, \mathbf{s})$  may contain multiple elements if there is more than one ISD measurement during period p at location  $\mathbf{s}$ . They may also be empty if there are no matching AIRS or CrIMSS footprints.

After creating  $\mathcal{A}^k(p, \mathbf{s})$  for all periods and ISD locations, we create supersets of matchup value pairs by combining across three-day moving windows, by mode:

$$\mathcal{A}^{kj}(d,\mathbf{s}) = \mathcal{A}^k(d-1,j,\mathbf{s}) \cup \mathcal{A}^k(d,j,\mathbf{s}) \cup \mathcal{A}^k(d+1,j,\mathbf{s}), \quad \mathcal{A}^{kj}(d) = \bigcup_{\mathbf{s}} \mathcal{A}^{kj}(d,\mathbf{s}).$$

 $j \in \{\text{day,night}\}$ . We chose the three-day time window after experimenting with shorter and longer windows. Shorter windows did not provide adequate sample sizes while longer windows failed to capture weather-related changes. Ideally, window duration would be as short as possible since longer time windows result in larger variance estimates in the fused data, relative to withheld ISD data. The final step before actually computing estimated bias and variance for each AIRS and CrIMSS footprint is to tessellate a 240 km (approximately two degrees), hexagonal spatial grid over CONUS. We do this by creating a discrete global grid using the DGGRID software package (Sahr et al., 2003; Sahr, 2019). One of the centers, for example, is at 87.72550324 W, 40.7908839 N, near Watseka, Illinois; this center uniquely determines the tessellated grid. All elements of  $\mathcal{A}^{kj}(d)$  are sorted in to these grid cells based on the instrument's footprint locations. Formally, let  $i \in 1, \ldots, L$  index grid cell centers, and let  $1_i(\mathbf{u}) = 1$  if  $\mathbf{u}$  lies inside cell *i*, and zero otherwise. For grid cell *i*, mode *j*, and date *d*, set

$$\mathcal{A}_i^{kj}(d) = \left\{ \left\{ Z^I\left(\mathbf{s}, t_m^I(\mathbf{s})\right), \, Z^k\left(\mathbf{u}_{m\mathbf{s}}^*, t^k(\mathbf{u}_{m\mathbf{s}}^*)\right) \, : \, \mathbf{1}_i(\mathbf{u}_{m\mathbf{s}}^*) = 1 \right\}_{m=1}^{M(d,j,\mathbf{s})} \right\}_{m=1}^{dl} \mathbf{s},$$

654 655 656 where  $M(d, j, \mathbf{s})$  is the number of time points acquired by the ISD station at  $\mathbf{s}$  on day d in mode j, L is the total number of hexagonal grid cells, and we write  $\mathbf{u}_{ms}^*$  to emphasize its dependence on m and  $\mathbf{s}$  via the matchup functions.

The bias assigned to all footprints from the k-th instrument observed on day d in mode j belonging to grid cell i is,

$$\mathbf{b}_{dji}^{k} = \frac{1}{|\mathcal{A}_{i}^{kj}(d)|} \sum_{all \ \mathbf{s}} \sum_{m=1}^{M(d,j,\mathbf{s})} \left[ Z^{k} \big( \mathbf{u}_{m\mathbf{s}}^{*}, t^{k}(\mathbf{u}_{m\mathbf{s}}^{*}) \big) - Z^{I} \big( \mathbf{s}, t_{m}^{I}(\mathbf{s}) \big) \right] \mathbf{1}_{i} \big( \mathbf{u}_{m\mathbf{s}}^{*} \big).$$

The corresponding variance assigned to all footprints observed on day d in mode j belonging to grid cell i is,

$$\mathbf{v}_{dji}^{k} = \frac{1}{|\mathcal{A}_{i}^{kj}(d)|} \sum_{all \ \mathbf{s}} \sum_{m=1}^{M(d,j,\mathbf{s})} \left[ Z^{k} \left( \mathbf{u}_{m\mathbf{s}}^{*}, t^{A}(\mathbf{u}_{m\mathbf{s}}^{*}) \right) - Z^{I} \left( \mathbf{s}, t_{m}^{I}(\mathbf{s}) \right) - \mathbf{b}_{dji}^{k} \right]^{2} \mathbf{1}_{i} \left( \mathbf{u}_{m\mathbf{s}}^{*} \right),$$

Subtracting the biases from the satellite footprints yields bias-corrected data. Denote an footprint acquired by the k-th instrument on day d in mode j, centered at location  $\mathbf{u}$ , by  $Z_{dj}^{A}(\mathbf{u})$ , where we suppress the argument  $t^{A}(\mathbf{u})$  since, for a given date and mode, location and time are confounded. The bias-corrected value is denoted by  $Z_{di}^{k*}(\mathbf{u})$  as follow:

$$Z_{dj}^{k*}\left(\mathbf{u}\right) = Z_{dj}^{A}\left(\mathbf{u}\right) - \mathbf{b}_{dji^{*}}^{A}, \quad i^{*} = \operatorname*{argmax}_{i} \mathbf{1}_{i}(\mathbf{u}),$$

with associated variance  $v_{dji^*}^k$ .

#### 658 References

- AIRS Project. (2019). Aqua/AIRS L2 Standard Physical Retrieval (AIRSonly) V7.0. Goddard Earth Sciences Data and Information Services Center (GES DISC). Greenbelt, MD, USA. (Accessed: 2019-2021) doi: 10.5067/VP1M6OG1X7M1
- AIRS Project. (2020). About the data. Retrieved 2021-12-26, from https://airs .jpl.nasa.gov/data/about-the-data/granules/
- Barnet, C. (2019). Sounder SIPS: Suomi NPP CrIMSS Level 2 CLIMCAPS normal
   spectral resolution: Cloud cleared radiances v2. Goddard Earth Sciences Data
   and Information Services Center (GES DISC). Greenbelt, MD, USA. (Accessed: 2019-2021) doi: 10.5067/CNG0ST72533Z
- Blackwell, W. (2005). A neural-network technique for the retrieval of atmospheric
   temperature and moisture profiles from high spectral resolution sounding data.
   *Geoscience and Remote Sensing, IEEE Transactions on*, 43(11), 2535-2546.
   doi: 10.1109/TGRS.2005.855071

673	Braverman, A., Hobbs, J., Teixeira, J., & Gunson, M. (2021). Post hoc uncertainty
674	quantification for remote sensing observing systems. SIAM/ASA Journal on
675	Uncertainty Quantification, $9(3)$ , $1064-1093$ .
676	Chahine, M. T., Pagano, T. S., Aumann, H. H., Atlas, R., Barnet, C., Blaisdell, J.,
677	Zhou, L. (2006). AIRS: Improving weather forecasting and providing new
678	data on greenhouse gases. Bulletin of the American Meteorological Society,
679	$\delta 7(1), 911-920.$
680	Cressie, N. (2013). Statistics for spatial data. John whey & Sons. Cressie N is Ishannagan $C_{-}(2008)$ Eirod contribution for some lange spatial data.
681	oressie, N., & Johannesson, G. (2008). Fixed rank kriging for very large spatial data
682 683	sets. Journal of the Hogai Statistical Society. Series D (Statistical Methodol- ogy), $70(1)$ , 209–226.
684	Ferguson, C. R., & Wood, E. F. (2010). An evaluation of satellite remote sensing
685	data products for land surface hydrology: Atmospheric infrared sounder. Jour-
686	nal of $Hydrometeorology$ , $11(6)$ , $1234-1262$ .
687	Ghamisi, P., Rasti, B., Yokoya, N., Wang, Q., Hofle, B., Bruzzone, L., others
688	(2019). Multisource and multitemporal data fusion in remote sensing: A
689	comprehensive review of the state of the art. <i>IEEE Geoscience and Remote</i>
690	Sensing Magazine, $7(1)$ , 6–39.
691	Gotway, C. A., & Young, L. J. (2002, June). Combining incompatible spatial data.
692	Journal of the American Statistical Association, 97, 632-648.
693	Hammerling, D. M., Michalak, A. M., & Kawa, S. R. (2012). Mapping of CO2 at
694	high spatiotemporal resolution using satellite observations: Global distribu-
695	tions from OCO-2. Journal of Geophysical Research: Atmospheres, 117(D6).
696	Harrison, G., & Burt, S. D. (2021). Quantifying uncertainties in climate data: mea-
697	surement limitations of naturally ventilated thermometer screens. Environmen-
698	Handerson H $k$ Searle S (1081) On deriving the inverse of a sum of matrices
699	The inderson, i.i., & Searle, S. (1981). On deriving the inverse of a sum of matrices.
700	SIAM Benneun 23 53-60
700	SIAM Review, 23, 53-60. Hennermann K & Berrisford P (2019) ERA5 data documentation ECMWF
700 701 702	SIAM Review, 23, 53-60. Hennermann, K., & Berrisford, P. (2019). ERA5 data documentation, ECMWF. Hobbs J. Braverman A. Cressie N. Granat, B. & Gunson M. (2017)
700 701 702 703	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017).</li> <li>Simulation-based uncertainty quantification for estimating atmospheric CO2</li> </ul>
700 701 702 703 704	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017).</li> <li>Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1),</li> </ul>
700 701 702 703 704 705	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017).</li> <li>Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> </ul>
700 701 702 703 704 705 706	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017).</li> <li>Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut,</li> </ul>
700 701 702 703 704 705 706 707	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017).</li> <li>Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at</li> </ul>
700 701 702 703 704 705 706 707 708	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017).</li> <li>Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616),</li> </ul>
700 701 702 703 704 705 706 707 708 709	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017).</li> <li>Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi:</li> </ul>
700 701 702 703 704 705 706 707 708 709 710	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017).</li> <li>Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> </ul>
700 701 702 703 704 705 706 707 708 709 710 711	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017). Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>711</li> <li>712</li> </ul>	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017). Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Asso-</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>711</li> <li>712</li> <li>713</li> </ul>	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017).</li> <li>Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Association, 107(499), 1004-1018. Retrieved from https://doi.org/10.1080/</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>711</li> <li>712</li> <li>713</li> <li>714</li> </ul>	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017).</li> <li>Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Association, 107(499), 1004-1018. Retrieved from https://doi.org/10.1080/01621459.2012.694717</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>711</li> <li>712</li> <li>713</li> <li>714</li> <li>715</li> </ul>	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017). Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Association, 107(499), 1004-1018. Retrieved from https://doi.org/10.1080/01621459.2012.694717</li> <li>Nguyen, H., Katzfuss, M., Cressie, N., &amp; Braverman, A. (2014). Spatio-temporal based of the statistical data fusion for emote sensing application for the statistical data fusion for the form https://doi.org/10.1080/01621459.2012.694717</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>710</li> <li>711</li> <li>712</li> <li>713</li> <li>714</li> <li>715</li> <li>716</li> </ul>	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017). Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Association, 107(499), 1004-1018. Retrieved from https://doi.org/10.1080/01621459.2012.694717 doi: 10.1080/01621459.2012.694717</li> <li>Nguyen, H., Katzfuss, M., Cressie, N., &amp; Braverman, A. (2014). Spatio-temporal data fusion for very large remote sensing datasets. Technometrics, 56(2), 174–185</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>711</li> <li>712</li> <li>713</li> <li>714</li> <li>715</li> <li>716</li> <li>717</li> </ul>	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017).</li> <li>Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Association, 107(499), 1004-1018. Retrieved from https://doi.org/10.1080/01621459.2012.694717 doi: 10.1080/01621459.2012.694717</li> <li>Nguyen, H., Katzfuss, M., Cressie, N., &amp; Braverman, A. (2014). Spatio-temporal data fusion for very large remote sensing datasets. Technometrics, 56(2), 174–185.</li> <li>Olcon F. T. Fishbein F. Manning F. &amp; Maddy F. (2017). AIPS/AMSU/HSP</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>711</li> <li>712</li> <li>713</li> <li>714</li> <li>715</li> <li>716</li> <li>717</li> <li>718</li> <li>710</li> </ul>	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017).</li> <li>Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Association, 107(499), 1004-1018. Retrieved from https://doi.org/10.1080/01621459.2012.694717</li> <li>Nguyen, H., Katzfuss, M., Cressie, N., &amp; Braverman, A. (2014). Spatio-temporal data fusion for very large remote sensing datasets. Technometrics, 56(2), 174–185.</li> <li>Olsen, E. T., Fishbein, E., Manning, E., &amp; Maddy, E. (2017). AIRS/AMSU/HSB Version 6 L2 product levels layers and trapezoids. Iet Promulsion Laboratory</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>711</li> <li>712</li> <li>713</li> <li>714</li> <li>715</li> <li>716</li> <li>717</li> <li>718</li> <li>719</li> <li>720</li> </ul>	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017). Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956-985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935-957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Asso- ciation, 107(499), 1004-1018. Retrieved from https://doi.org/10.1080/ 01621459.2012.694717 doi: 10.1080/01621459.2012.694717</li> <li>Nguyen, H., Katzfuss, M., Cressie, N., &amp; Braverman, A. (2014). Spatio-temporal data fusion for very large remote sensing datasets. Technometrics, 56(2), 174- 185.</li> <li>Olsen, E. T., Fishbein, E., Manning, E., &amp; Maddy, E. (2017). AIRS/AMSU/HSB Version 6 L2 product levels, layers and trapezoids. Jet Propulsion Laboratory, Pasadema CA USA</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>710</li> <li>711</li> <li>712</li> <li>713</li> <li>714</li> <li>715</li> <li>716</li> <li>717</li> <li>718</li> <li>719</li> <li>720</li> <li>721</li> </ul>	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017). Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Association, 107(499), 1004-1018. Retrieved from https://doi.org/10.1080/01621459.2012.694717</li> <li>Nguyen, H., Katzfuss, M., Cressie, N., &amp; Braverman, A. (2014). Spatio-temporal data fusion for very large remote sensing datasets. Technometrics, 56(2), 174–185.</li> <li>Olsen, E. T., Fishbein, E., Manning, E., &amp; Maddy, E. (2017). AIRS/AMSU/HSB Version 6 L2 product levels, layers and trapezoids. Jet Propulsion Laboratory, Pasadena, CA, USA.</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>711</li> <li>712</li> <li>713</li> <li>714</li> <li>715</li> <li>716</li> <li>717</li> <li>718</li> <li>719</li> <li>720</li> <li>721</li> <li>722</li> </ul>	<ul> <li>SIAM Review, 23, 53-00.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017). Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956-985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935-957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Asso- ciation, 107(499), 1004-1018. Retrieved from https://doi.org/10.1080/ 01621459.2012.694717 doi: 10.1080/01621459.2012.694717</li> <li>Nguyen, H., Katzfuss, M., Cressie, N., &amp; Braverman, A. (2014). Spatio-temporal data fusion for very large remote sensing datasets. Technometrics, 56(2), 174- 185.</li> <li>Olsen, E. T., Fishbein, E., Manning, E., &amp; Maddy, E. (2017). AIRS/AMSU/HSB Version 6 L2 product levels, layers and trapezoids. Jet Propulsion Laboratory, Pasadena, CA, USA.</li> <li>Sahr, K. (2019). Dggrid version 7.0: User documentation for discrete global grid software.</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>711</li> <li>712</li> <li>713</li> <li>714</li> <li>715</li> <li>716</li> <li>717</li> <li>718</li> <li>719</li> <li>720</li> <li>721</li> <li>722</li> <li>723</li> </ul>	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017). Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956-985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935-957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Asso- ciation, 107(499), 1004-1018. Retrieved from https://doi.org/10.1080/ 01621459.2012.694717 doi: 10.1080/01621459.2012.694717</li> <li>Nguyen, H., Katzfuss, M., Cressie, N., &amp; Braverman, A. (2014). Spatio-temporal data fusion for very large remote sensing datasets. Technometrics, 56(2), 174- 185.</li> <li>Olsen, E. T., Fishbein, E., Manning, E., &amp; Maddy, E. (2017). AIRS/AMSU/HSB Version 6 L2 product levels, layers and trapezoids. Jet Propulsion Laboratory, Pasadena, CA, USA.</li> <li>Sahr, K. (2019). Dggrid version 7.0: User documentation for discrete global grid software.</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>711</li> <li>712</li> <li>713</li> <li>714</li> <li>715</li> <li>716</li> <li>717</li> <li>718</li> <li>719</li> <li>720</li> <li>721</li> <li>722</li> <li>723</li> <li>724</li> </ul>	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017). Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Association, 107(499), 1004-1018. Retrieved from https://doi.org/10.1080/01621459.2012.694717</li> <li>Nguyen, H., Katzfuss, M., Cressie, N., &amp; Braverman, A. (2014). Spatio-temporal data fusion for very large remote sensing datasets. Technometrics, 56(2), 174-185.</li> <li>Olsen, E. T., Fishbein, E., Manning, E., &amp; Maddy, E. (2017). AIRS/AMSU/HSB Version 6 L2 product levels, layers and trapezoids. Jet Propulsion Laboratory, Pasadena, CA, USA.</li> <li>Sahr, K. (2019). Dggrid version 7.0: User documentation for discrete global grid software.</li> <li>Sahr, K., White, D., &amp; Kimerling, A. J. (2003). Geodesic discrete global grid systems. Cartography and Geographic Information Science, 30(2), 121-134.</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>711</li> <li>712</li> <li>713</li> <li>714</li> <li>715</li> <li>716</li> <li>717</li> <li>718</li> <li>719</li> <li>720</li> <li>721</li> <li>722</li> <li>723</li> <li>724</li> <li>725</li> </ul>	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017). Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Association, 107(499), 1004-1018. Retrieved from https://doi.org/10.1080/01621459.2012.694717</li> <li>Nguyen, H., Katzfuss, M., Cressie, N., &amp; Braverman, A. (2014). Spatio-temporal data fusion for very large remote sensing datasets. Technometrics, 56(2), 174–185.</li> <li>Olsen, E. T., Fishbein, E., Manning, E., &amp; Maddy, E. (2017). AIRS/AMSU/HSB Version 6 L2 product levels, layers and trapezoids. Jet Propulsion Laboratory, Pasadena, CA, USA.</li> <li>Sahr, K. (2019). Dggrid version 7.0: User documentation for discrete global grid software.</li> <li>Sahr, K., White, D., &amp; Kimerling, A. J. (2003). Geodesic discrete global grid systems. Cartography and Geographic Information Science, 30(2), 121–134.</li> <li>Smith, A., Lott, N., &amp; Vose, R. (2011). The integrated surface database: Recent de-</li> </ul>
<ul> <li>700</li> <li>701</li> <li>702</li> <li>703</li> <li>704</li> <li>705</li> <li>706</li> <li>707</li> <li>708</li> <li>709</li> <li>710</li> <li>711</li> <li>712</li> <li>713</li> <li>714</li> <li>715</li> <li>716</li> <li>717</li> <li>718</li> <li>719</li> <li>720</li> <li>721</li> <li>722</li> <li>723</li> <li>724</li> <li>725</li> <li>726</li> </ul>	<ul> <li>SIAM Review, 23, 53-60.</li> <li>Hennermann, K., &amp; Berrisford, P. (2019). ERA5 data documentation, ECMWF.</li> <li>Hobbs, J., Braverman, A., Cressie, N., Granat, R., &amp; Gunson, M. (2017). Simulation-based uncertainty quantification for estimating atmospheric CO2 from satellite data. SIAM/ASA Journal on Uncertainty Quantification, 5(1), 956–985.</li> <li>Mcnally, A. P., Watts, P. D., A. Smith, J., Engelen, R., Kelly, G. A., Thépaut, J. N., &amp; Matricardi, M. (2006). The assimilation of airs radiance data at ecmwf. Quarterly Journal of the Royal Meteorological Society, 132(616), 935–957. Retrieved from http://dx.doi.org/10.1256/qj.04.171 doi: 10.1256/qj.04.171</li> <li>Nguyen, H., Cressie, N., &amp; Braverman, A. (2012). Spatial statistical data fusion for remote sensing applications. Journal of the American Statistical Association, 107(499), 1004-1018. Retrieved from https://doi.org/10.1080/01621459.2012.694717</li> <li>Nguyen, H., Katzfuss, M., Cressie, N., &amp; Braverman, A. (2014). Spatio-temporal data fusion for very large remote sensing datasets. Technometrics, 56(2), 174-185.</li> <li>Olsen, E. T., Fishbein, E., Manning, E., &amp; Maddy, E. (2017). AIRS/AMSU/HSB Version 6 L2 product levels, layers and trapezoids. Jet Propulsion Laboratory, Pasadena, CA, USA.</li> <li>Sahr, K. (2019). Dggrid version 7.0: User documentation for discrete global grid systems. Cartography and Geographic Information Science, 30(2), 121–134.</li> <li>Smith, A., Lott, N., &amp; Vose, R. (2011). The integrated surface database: Recent developments and partnerships. Bulletin of the American Meteorological Society, version 4, partnerships. Bulletin of the American Meteorological Society, version 4, partnerships. Bulletin of the American Meteorological Society, velopments and partnerships. Bulletin of the American Meteorological Society, velopments and partnerships. Bulletin of the American Meteorological Society, velopments</li> </ul>

700	Smith N & Barnot C D $(2010)$ . Uncortainty characterization and propagation
728	in the Community Long Term Infrared Microwaya Combined Atmospheric
729	Product System (CLIMCAPS) Remote Sensing 11(10) 1997
730	Smith N & Barnot C D (2020) CLIMCAPS absorving capability for tempor
731	ature moisture and trace gases from AIRS/AMSU and CrIS/ATMS
732	and chief and trace gases from Anto AMSC and Chief ATMS. Atmo-
/33	Sun I McColl K A Wang V Bigdon A I Lu H Vang K Santanollo Ir
734	I = A = (2021) Clobal evaluation of terrestrial near surface air temperature
735	and specific humidity retrievals from the atmospheric infrared sounder (airs)
730	Remote Sensing of Environment 252 112146
737	Susskind I Blaisdell I M & Iredell I. (2014) Improved methodology for
738	surface and atmospheric soundings error estimates and quality control pro-
739	codures: the atmospheric infrared sounder science team version 6 retrieval
740	algorithm <i>Journal of Applied Remate Sensing</i> 8(1) 084994 Retrieved from
741	http://dx doi_org/10_1117/1_IBS_8_084994_doi: 10_1117/1_IBS_8_084994
742	Thrastarson H T Manning E Kahn B Fetzer E Yue O Wong S others
744	(2020). AIRS/AMSU/HSB Version 7 Level 2 product user guide. Jet Promil-
745	sion Laboratory, California Institute of Technology: Pasadena, CA, USA,
746	83–92.
747	Wilks, D. S. (2006). Statistical methods in the atmospheric sciences (Second ed.).
748	Academic Press.
749	Yue, Q., Lambrigtsen, B., et al. (2017). AIRS V6 test report supplement: Perfor-
750	mance of AIRS+AMSU vs. AIRS-only retrievals. Jet Propulsion Laboratory,
751	California Institute of Technology: Pasadena, CA, USA. Retrieved from
752	https://docserver.gesdisc.eosdis.nasa.gov/repository/Mission/
753	AIRS/3.3_ScienceDataProductDocumentation/3.3.5_ProductQuality/
754	V6_Test_Report_Supplement_Performance_of_AIRS+AMSU_vs_AIRS-Only
755	_Retrievals.pdf
756	Yue, Q., Lambrigtsen, B., et al. (2020). AIRS V7 L2 performance test and vali-
757	dation report. Jet Propulsion Laboratory, California Institute of Technology:
758	Pasadena, CA, USA. Retrieved from https://docserver.gesdisc.eosdis
759	.nasa.gov/public/project/AIRS/V7_L2_Performance_Test_and_Validation
760	_report.pdf
761	Yue, Q., Lambrigtsen, B., et al. (2021). Version 2 CLIMCAPS-Aqua re-
762	trieval product performance test report. Jet Propulsion Laboratory, Cal-
763	ifornia Institute of Technology: Pasadena, CA, USA. Retrieved from
764	https://docserver.gesdisc.eosdis.nasa.gov/public/project/Sounder/

https://docserver.gesdisc.eosdis. CLIMCAPS.V2.Test.Report.Aqua.pdf 765